

# Capabilities for Effects

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Formalism by Aaron Craig as Undergraduate Thesis student at VUW in 2017/2018

# CAPABILITY-FLAVOURED EFFECTS

# Capability Safety

- Capability-safe languages prohibit ambient authority
  - All authority derives from previous authority, starting at the entry point of the program
  - A component can't exercise authority unless you give it a capability to do so
- Can be used to quantify risk of executing code [Drossopolou] and ensure least privilege [Saltzer]
- Do capabilities help existing formal reasoning techniques, such as effects?

# Effects

- Describe “intensional information” about how a program executes (Neilson & Nelson)
  - $Int \rightarrow Int$  (unannotated function type)
  - $Int \{-File.write\} \rightarrow Int$  (annotated function type)
- Limited mainstream use; too verbose? (Rytz)
- Inference helps reduce verbosity
  - Need to analyse source code
  - Back to manual reasoning if it fails

# Capability-Flavoured Effects

- In a capability-safe setting, any effect on a resource must happen through a capability
- By tracking capabilities, we also track effects
- What can we say at the boundary where annotated code passes capabilities into unannotated code?

- ```
import(File.append)
  logger: String -{File.append}→ Unit
in
  e // arbitrary, unannotated code
```

# Capability-Flavoured Effects

- Can safely determine effects of unannotated code by inspecting the capabilities we give it
  - Only have to inspect its type, not its source code
- Effect-conscious capability-safe code can reason about what untrusted, capability-safe code will do
- Our work: formulates a minimal, sound lambda calculus and type system to demonstrate this

# Imports

```
import(File.append)
  log: String -{File.append}→ Unit
in
  log(“doing some logging”)
```

- Pass in capabilities, execute unannotated code
- Unannotated code must type with *exactly* the free variables imported
- Programmer *selects* authority as `{File.*}`
- Statically: accept/reject, if `{File.*}` is a safe upper-bound on effects

# Multiple Imports

```
import(File.*)
  makeFile: Unit -{File.create}→ Unit
  pureApply: (Unit -∅→ Unit) -∅→ Unit
in
  pureApply(makeFile)
```

- Input to `pureApply` has same type as `makeFile` (modulo effect annotations)
- Don't want `pureApply` to violate its annotation by incurring a `File.create` effect in the unannotated code
- Need to ensure all imports are allowed the selected authority before passing them in



# Higher-Order Effects

- Regular effect: you possess capability for effect
- Higher-order effect: allowed to incur effect, but you need to be given the capability

```
... // some omitted set up code
def log(msg: String, sock: Socket) =
  file.append("hello")
  sock.append("they're logging")
```

- Assuming this typechecks...
  - `File.append` is a regular effect
  - `Socket.append` is higher order

# Higher-Order Safety

- An annotated type  $\tau$  is *higher-order safe* for a set of effects  $\varepsilon$  if  $\varepsilon \subseteq \text{ho-effects}(\tau)$
- Intuitively: an expression of type  $\tau$  must be allowed to incur the effects in  $\varepsilon$
- To safely check an import, all imports must be higher-order safe for the selected authority

```
import(File.create)
  makeFile: Unit -{File.create}→ Unit
  pureApply: (Unit -∅→ Unit) -∅→ Unit
in
  pureApply(log)
```

# Return Types

- Unannotated code might return a function/capability
- Need to annotate it with effects to safely effect-check rest of annotated code

```
let result =  
  import(File.*)  
  f: {File}  
  in  
    def tricky(): Unit =  
      f.write("hello")  
  result()
```

- The type of tricky is  $\text{Unit} \rightarrow \text{Unit}$ , which annotates as  $\text{Unit} \text{-}\{\text{File}.*\}\rightarrow \text{Unit}$

# Return Types

- Unannotated code might return a function that can later be used elsewhere in the annotated world
- Need to understand what effects it has to safely effect-check annotated code using it

```
import(File.*)  
  f: {File}  
  
in  
  
  def tricky(): Unit =  
    f.write("hello")
```

- The type of `tricky` is `Unit → Unit`, which annotates as `Unit -{File.*}→ Unit`

# Returning Higher-Order Effects

```
import(File.*)
  f: {File}

in
  def myFunc(msg: String, s: Socket): Unit =
    s.write("they're logging")
    f.write(msg)
```

- Safe to execute this code
- Unsafe to annotate return type with `{File.*}`
- Must make sure return type doesn't ask for a capability (`Socket`) whose effects haven't been selected
  - This example rejects because `String → Socket → Unit` has the higher-order effects `{Socket.*}`

# Polymorphic Types

- Polymorphic types let you write type-generic code
- Polymorphic effects let you write effect-generic code

```
// Define a new effect to simplify function definition
effect write = {File.write, Socket.write}

// Takes a write function, uses it to write a message, logs
def writeData< $\varphi \subseteq$  write>(s: String, write: String  $-\varphi \rightarrow$  Unit) =
  write(s)
  file.append("wrote to writer")

type WriteDataFunc = typeof(writeData)
```

# Polymorphic Imports

```
effect write = {File.write, Socket.write}
import(File.append, File.write, Socket.write)
  writeData: WriteDataFunc<write>
  fwriter: String -{File.write, File.append}-> Unit
in
  e
```

- Can approximate effects of `writeData` with its polymorphic upper bound `{File.write, Socket.write}`
- Can approximate effects of the unannotated code as `{File.append, File.write, Socket.write}`

# Polymorphic Imports

- Lots of generic code doesn't have an upper bound on its possible effects
  - map, fold/reduce, filter, zip, collections
- To incur an effect with generics you must instantiate with something concrete that can invoke the effect
  - Capability for the effect must have been imported
- Can tighten the upper-bound by looking at other capabilities that have been imported



# Polymorphic Imports

```
effect write = {File.write, Socket.write}
import(File.append, File.write, Socket.write)
  writeData: WriteDataFunc<write>
  fwriter: String -{File.write, File.append}-> Unit
in
  e
```

- Nothing imported can incur `Socket.write` so we can ignore that as a possibility for `writeData`
- Upper-bound on `writeData` tightens to `{File.write}`
- Better approximation of effects of `e` is `{File.write, File.append}`

# Overall

- Capability-safe design enables reasoning at module boundaries about the effects of unannotated code
- Must restrict capabilities passed in based on their higher-order effects
- Finer reasoning needed for useful polymorphics

Paper by Aaron Craig, Alex Potanin, Lindsay Groves, and Jonathan Aldrich  
at ICFEM 2018 conference

# CAPABILITIES: EFFECTS FOR FREE

# Motivation

- Consider a program which calls a logger component:

```
1 module def logger(f:{File}):Logger
2 def log(x: String): Unit
```

```
1 module def client(logger: Logger)
2 def run(): Unit = logger.log(x)
```

- We pass the logger a file expecting it to append to it.
  - But how do we ensure that is all it does?
- In Java, once the logger has the file, it can do anything it wants: “ambient authority”.
- Capabilities have been used informally to reason about resource use — can we use them formally?

# Approach

- We look at adding capability-based reasoning to a formal system for reasoning about resource use.
- Specifically, a small effect calculus based on the  $\lambda$ -calculus, with operations on resources.
- Rich enough to capture examples written in a subset of a capability-safe language, Wyvern.
- Look at how we can minimise the need for effect annotations in order to make such a system easier to use.
- Using capabilities allows us to bound the effects of unannotated code without needing to annotate it.

# Basic Language

We start with a very simple language with operations on resources.

|     |                       |                         |          |                         |                     |
|-----|-----------------------|-------------------------|----------|-------------------------|---------------------|
| $e$ | $::=$                 | <i>exprs :</i>          | $\tau$   | $::=$                   | <i>types :</i>      |
|     | $x$                   | <i>variable</i>         |          | $\{\bar{r}\}$           | <i>resource set</i> |
|     | $v$                   | <i>value</i>            |          | $\tau \rightarrow \tau$ | <i>function</i>     |
|     | $e e$                 | <i>application</i>      |          |                         |                     |
|     | $e.\pi$               | <i>operation</i>        |          |                         |                     |
|     |                       |                         | $\Gamma$ | $::=$                   | <i>type ctx :</i>   |
| $v$ | $::=$                 | <i>values :</i>         |          | $\emptyset$             | <i>empty ctx</i>    |
|     | $r$                   | <i>resource literal</i> |          | $\Gamma, x : \tau$      | <i>binding</i>      |
|     | $\lambda x : \tau. e$ | <i>abstraction</i>      |          |                         |                     |

- Semantics uses reduction relation  $e \longrightarrow e$  (ignoring operations).
- Type system has judgements:  $\Gamma \vdash e : \tau$ .
- Shows types of inputs and outputs, but nothing about effects.

# Adding Effects

Add annotations to function types to show the effects that *may* occur.

|     |                       |                         |               |                                       |                     |
|-----|-----------------------|-------------------------|---------------|---------------------------------------|---------------------|
| $e$ | $::=$                 |                         | $\tau$        | $::=$                                 |                     |
|     | $x$                   | <i>exprs :</i>          |               | $\{\bar{r}\}$                         | <i>types :</i>      |
|     | $v$                   | <i>variable</i>         |               | $\tau \rightarrow_{\varepsilon} \tau$ | <i>resource set</i> |
|     | $e e$                 | <i>value</i>            |               |                                       | <i>function</i>     |
|     | $e.\pi$               | <i>application</i>      | $\Gamma$      | $::=$                                 | <i>type ctx :</i>   |
|     |                       | <i>operation</i>        |               | $\emptyset$                           | <i>empty ctx.</i>   |
|     |                       |                         |               | $\Gamma, x : \tau$                    | <i>binding</i>      |
| $v$ | $::=$                 | <i>values :</i>         |               |                                       |                     |
|     | $r$                   | <i>resource literal</i> | $\varepsilon$ | $::=$                                 | <i>effects :</i>    |
|     | $\lambda x : \tau. e$ | <i>abstraction</i>      |               | $\{\overline{r.\pi}\}$                | <i>effect set</i>   |

Effects are sets of resource-operation pairs.

# Adding Effects

- Semantics uses reduction relation  $e \longrightarrow e \mid \varepsilon$ , where  $\varepsilon$  is the effects that occur during evaluation of  $e$ .
- Type/effect system has judgements:  $\Gamma \vdash e : \tau$  with  $\varepsilon$ .  
So we can check what effects may occur during evaluation of  $e$ .
- But this requires extensive annotation, which is tedious in practice.  
E.g. Java unchecked exceptions are often criticised and often misused.
- Also, we may want to import third-party code which is not annotated.



# Adding Capabilities

- Key idea is to combine annotated and unannotated code.
  - Allow annotated code to import unannotated code.
  - passing it the capabilities (resources) it needs.
  - and specifying the effects they are permitted to have.
- Combine the languages of unannotated and annotated code. using hat (e.g.  $\hat{e}$ ) in the formalism to distinguish them.
- Add a new statement:  $\text{import}(\varepsilon_s) x = \hat{e} \text{ in } e$ 
  - $e$  is the unannotated code being imported
  - $\hat{e}$  is the capability being passed to  $e$ , which is bound to  $x$  in  $e$ .
  - $\varepsilon_s$  is the set of effects which  $e$  is allowed to have (“selected authority”).
- E.g.  $\text{import}(\text{File.append}) x = \text{File} \text{ in } \lambda y : \text{Unit}. x.\text{write}.$ 

This logger exceeds its authority so will be rejected!

# Adding Capabilities

- Semantics uses reduction relation  $\hat{e} \longrightarrow \hat{e} \mid \varepsilon$ .

We are only concerned with executing annotated code.

- To execute unannotated code which is imported, we annotate it with the selected authority.

$$\frac{}{\text{import}(\varepsilon_s) \ x = \hat{v} \ \text{in} \ e \longrightarrow [\hat{v}/x] \text{annot}(e, \varepsilon_s) \mid \emptyset} \text{(E-IMPORT2)}$$

- $\text{annot}(e, \varepsilon_s)$  just adds  $\varepsilon_s$  to function arrows in  $e$ .

# Example: Importing Logger

```
1 let MakeLogger =  
2   ( $\lambda$ f: File.  
3     import (File.append) f = f in  
4      $\lambda$ x: Unit. f.append) in  
5  
6 let MakeClient =  
7   ( $\lambda$ logger: Logger.  
8      $\lambda$ x: Unit. logger unit) in  
9  
10 let MakeMain =  
11   ( $\lambda$ f: File.  
12     let loggerModule = MakeLogger f in  
13     let clientModule = MakeClient loggerModule in  
14     clientModule unit) in  
15  
16 MakeMain File
```

**Note:** `let` expression is usual syntactic sugar.

# Example: Higher Order Effects

```
1 let malicious =  
2   (import (∅) y=unit in  
3     λf: Unit → Unit. f()) in  
4  
5 let plugin =  
6   (λf: {File}.  
7     malicious(λx:Unit. f.read)) in  
8  
9 let MakeMain =  
10  (λf: {File}.  
11    plugin f) in  
12  
13 MakeMain File
```

# Type and Effect Checking for Imports

Most type and effect rules are straightforward, but...

For import, we want a rule of the form:

$$\frac{\dots}{\hat{\Gamma} \vdash \text{import}(\varepsilon_s) x = \hat{e} \text{ in } e : \dots \text{ with } \dots} (\varepsilon\text{-IMPORT})$$

- What type and effects does the import expression have?
- What assumptions do we need?

# Typing Imports – First Attempt

$$\frac{\hat{\Gamma} \vdash \hat{e} : \hat{\tau} \text{ with } \varepsilon_1 \quad x : \text{erase}(\hat{\tau}) \vdash e : \tau}{\hat{\Gamma} \vdash \text{import}(\varepsilon_S) x = \hat{e} \text{ in } e : \text{annot}(\tau, \varepsilon_S) \text{ with } \varepsilon_S \cup \varepsilon_1} \quad (\varepsilon\text{-IMPORT1})$$

- Assume arbitrary type and effect for  $\hat{e}$ .
- Must be able to type  $e$ , given just that  $x$  has type  $\hat{\tau}$ , to ensure  $e$  uses only the capabilities provided to it.
- $e$  is unannotated while  $\hat{\tau}$  is annotated, so we erase the annotations from  $\hat{\tau}$ .
- $e$  has type  $\tau$  — but  $\tau$  is unannotated, so we annotate with  $\varepsilon_S$ .
- Evaluating  $e$  has all effects in  $\varepsilon_1$  and  $\varepsilon_S$ .

# Typing Imports – Second Attempt

$$\frac{\hat{\Gamma} \vdash \hat{e} : \hat{\tau} \text{ with } \varepsilon_1 \quad x : \underline{\text{erase}(\hat{\tau})} \vdash e : \tau \quad \boxed{\text{effects}(\hat{\tau}) \subseteq \varepsilon_s}}{\hat{\Gamma} \vdash \text{import}(\varepsilon_s) x = \hat{e} \text{ in } e : \text{annot}(\tau, \varepsilon_s) \text{ with } \varepsilon \cup \varepsilon_1} \quad (\varepsilon\text{-IMPORT2})$$

- First version allows any capability to be passed to  $e$ .
- Restrict  $\hat{e}$  so that its effects are contained in  $\varepsilon_s$ .
- *effects* collects all the effects captured by its argument.

$$\text{effects}(\{\bar{r}\}) = \{r.\pi \mid r \in \bar{r}, \pi \in \Pi\}$$

$$\text{effects}(\hat{\tau}_1 \rightarrow_\varepsilon \hat{\tau}_2) = \text{effects}(\hat{\tau}_1) \cup \varepsilon \cup \text{effects}(\hat{\tau}_2)$$

```
1 import ({File.*})
2   go =  $\lambda x$ : Unit  $\rightarrow_{\emptyset}$  Unit. x unit
3   f = File
4 in
5   go ( $\lambda y$ : Unit. f.write)
```

# Typing Imports – Third Attempt

$$\frac{\hat{\Gamma} \vdash \hat{e} : \hat{\tau} \text{ with } \varepsilon_1 \quad \text{effects}(\hat{\tau}) \subseteq \varepsilon_s \quad \boxed{\text{ho-safe}(\hat{\tau}, \varepsilon_s)} \quad x : \text{erase}(\hat{\tau}) \vdash e : \tau}{\hat{\Gamma} \vdash \text{import}(\varepsilon_s) \ x = \hat{e} \text{ in } e : \text{annot}(\tau, \varepsilon_s) \text{ with } \varepsilon \cup \varepsilon_1} \quad (\varepsilon\text{-IMPORT3})$$

$$\text{effects}(\{\bar{r}\}) = \{r.\pi \mid r \in \bar{r}, \pi \in \Pi\}$$

$$\text{effects}(\hat{\tau}_1 \rightarrow_\varepsilon \hat{\tau}_2) = \text{ho-effects}(\hat{\tau}_1) \cup \varepsilon \cup \text{effects}(\hat{\tau}_2)$$

$$\text{ho-effects}(\{\bar{r}\}) = \emptyset$$

$$\text{ho-effects}(\hat{\tau}_1 \rightarrow_\varepsilon \hat{\tau}_2) = \text{effects}(\hat{\tau}_1) \cup \text{ho-effects}(\hat{\tau}_2)$$

- Need to distinguish “direct” effects from “higher-order” effects.
- And ensure safe use of resources: imported capabilities must be expecting the effects they are passed by unannotated code.



# Typing Imports – Fourth (and Final) Attempt

$$\boxed{\text{effects}(\hat{\tau}) \cup \text{ho-effects}(\text{annot}(\tau, \emptyset)) \subseteq \varepsilon_s}$$

$$\frac{\hat{\Gamma} \vdash \hat{e} : \hat{\tau} \text{ with } \varepsilon_1 \quad \text{ho-safe}(\hat{\tau}, \varepsilon_s) \quad x : \text{erase}(\hat{\tau}) \vdash e : \tau}{\hat{\Gamma} \vdash \text{import}(\varepsilon_s) x = \hat{e} \text{ in } e : \text{annot}(\tau, \varepsilon_s) \text{ with } \varepsilon_s \cup \varepsilon_1} \quad (\varepsilon\text{-IMPORT})$$

Distinction between direct and higher-order effects needs to be pushed further!

$$\boxed{\text{safe}(\hat{\tau}, \varepsilon)}$$

$$\frac{\{r.\pi \mid r \in \bar{r}, \pi \in \Pi\} \subseteq \varepsilon}{\text{safe}(\hat{\tau}, \varepsilon)} \quad (\text{SAFE-RESOURCE})$$

$$\frac{\varepsilon \subseteq \varepsilon' \quad \text{ho-safe}(\hat{\tau}_1, \varepsilon) \quad \text{safe}(\hat{\tau}_2, \varepsilon)}{\text{safe}(\hat{\tau}_1 \rightarrow_{\varepsilon'} \hat{\tau}_2, \varepsilon)} \quad (\text{SAFE-ARROW})$$

$$\boxed{\text{ho-safe}(\hat{\tau}, \varepsilon)}$$

$$\frac{}{\text{ho-safe}(\{\bar{r}\}, \varepsilon)} \quad (\text{HOSAFE-RESOURCE})$$

$$\frac{\text{safe}(\hat{\tau}_1, \varepsilon) \quad \text{ho-safe}(\hat{\tau}_2, \varepsilon)}{\text{ho-safe}(\hat{\tau}_1 \rightarrow_{\varepsilon'} \hat{\tau}_2, \varepsilon)} \quad (\text{HOSAFE-ARROW})$$

# Conclusions

- We can now check examples like the ones given earlier and safely reject ones that violate the granted authority.
- Doesn't require programmers to add effect annotations.
- Relies on type checking, not effect checking — doesn't require unannotated expressions to be analysed for their effects.

Implementation by Justin Lubin as Undergraduate RA at CMU in the summer of 2018

# APPROXIMATING POLYMORPHIC EFFECTS WITH CAPABILITIES

# Goal

Allow *secure* and *ergonomic* mixing of effect-unannotated code with effect-annotated code in a *realistic* capability-safe programming language.

# Object Capabilities

## *Capabilities*

Unforgeable objects that give particular parts of the code access to sensitive resources

## *Capability-safe language*

A language in which the only way to access sensitive resources is via capabilities

```
module def logger(myFile : File)
  ...

module def main(platform : Platform)
  val myFile = file(platform)
  val myLogger = logger(myFile)
  ...
```

# Effect Systems

## *Effect system*

Annotations on methods describing effects they can incur

## *Capability-based effect system*

Way of formally reasoning about capabilities (*awesome!*)

***Downside:*** verbosity

# Capability-Safe Import Semantics

*Prior work (Craig et al.)*

Import semantics for capability-safe lambda calculus

*Limitation*

Does not handle mutable state nor effect polymorphism

*Our goal*

Scale up to a more realistic programming language

# The Problem

Effect polymorphism *and* mutability



# The Problem

```
resource type Logger
  effect log
  def append(contents : String) : {log} Unit

module def reversePlugin(name : String)
  var logger : Logger = ...
  def setLogger(newLogger : Logger) : Unit
    logger = newLogger
  def run(s : String) : String
    val t = s.reverse()
    logger.append(name + ":" + s + " -> " + t)
  t
```

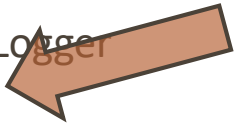
**Question:** *How will annotated code use `reversePlugin`?*

Effect polymorphism + mutability  
⇒ **log** effect could be *anything!*

# The Problem

```
resource type Logger
  effect log
  def append(contents : String) : {log} Unit

module def reversePlugin(name : String)
  var logger : Logger = ...
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    logger = newLogger
  def run(s : String) : String
    val t = s.reverse()
    logger.append(name + ":" + s + " ->" + t)
  t
```



**Question:** *How will annotated code use `reversePlugin`?*

Effect polymorphism + mutability  
⇒ **log** effect could be *anything!*

# The Problem

```
resource type Logger
  effect log
  def append(contents : String) : {log} Unit

module def reversePlugin(name : String)
  var logger : Logger = ...
  def setLogger(newLogger : Logger) : Unit
    logger = newLogger
  def run(s : String) : String
    val t = s.reverse()
    logger.append(name + ":" + s + " ->" + t)
  t
```

**Question:** *How will annotated code use `reversePlugin`?*

Effect polymorphism + mutability  
⇒ **log** effect could be *anything!*

# Solution

Quantification lifting

# Quantification Lifting: Idea

```
resource type Logger
  effect log
  def append(contents : String) : {log} Unit

module def reversePlugin(name : String)
  var logger : Logger = ...
  def setLogger(newLogger : Logger) : Unit
    logger = newLogger
  def run(s : String) : String
    val t = s.reverse()
    logger.append(name + ":" + s + "->" + t)
  t
```

```
resource type Logger[effect E]
  def append(contents : String) : {E} Unit

module def reversePlugin[effect E](name : String)
  var logger : Logger[E] = ...
  def setLogger(newLogger : Logger[E]) : {E} Unit
    logger = newLogger
  def run(s : String) : {E} String
    val t = s.reverse()
    logger.append(name + ":" + s + "->" + t)
  t
```

- *Lift* effect polymorphism from inside ML-style module functor to the functor itself
- Collapse each universal effect quantification into single quantified effect E
  - Serves as effect bound for all methods in module


# Quantification Lifting: Idea

```
resource type Logger
  effect log
  def append(contents : String) : {log} Unit

module def reversePlugin(name : String)
  var logger : Logger = ...
  def setLogger(newLogger : Logger) : Unit
    logger = newLogger
  def run(s : String) : String
    val t = s.reverse()
    logger.append(name + ": " + s + " -> " + t)
  t
```

```
resource type Logger[effect E]
  def append(contents : String) : {E} Unit

module def reversePlugin[effect E](name : String)
  var logger : Logger[E] = ...
  def setLogger(newLogger : Logger[E]) : {E} Unit
    logger = newLogger
  def run(s : String) : {E} String
    val t = s.reverse()
    logger.append(name + ": " + s + " -> " + t)
  t
```



- *Lift* effect polymorphism from inside ML-style module functor to the functor itself
- Collapse each universal effect quantification into single quantified effect E
  - Serves as effect bound for all methods in module

# Quantification Lifting: Usage

```
import fileLogger, databaseLogger, reversePlugin
val logger1 = fileLogger(...)
val logger2 = databaseLogger(...)
val plugin = reversePlugin[logger1.log]("archive")
def main() : {logger1.log} Unit
  plugin.setLogger(logger1)
  // plugin.setLogger(logger2) <-- not allowed!
```

```
resource type MyPlugin
  def setLogger(newLogger : Logger') : {logger1.log} Unit
  def run(s : String) : {logger1.log} String

resource type Logger'
  effect log = {logger1.log}
  def append(contents : String) : {log} Unit
```

# Quantification Lifting: Import Bounds

```
resource type Logger
  effect log
  def append(contents : String) : {log} Unit

module def reversePlugin(name : String)
  var logger : Logger = ...
  def setLogger(newLogger : Logger) : Unit
    logger = newLogger
  def run(s : String) : String
    val t = s.reverse()
    logger.append(name + ":" + s + "->" + t)
  t
```

```
resource type Logger[effect E]
  def append(contents : String) : {E} Unit

module def reversePlugin[effect E](name : String)
  var logger : Logger[E] = ...
  def setLogger(newLogger : Logger[E]) : {E} Unit
    logger = newLogger
  def run(s : String) : {E} String
    val t = s.reverse()
    logger.append(name + ":" + s + "->" + t)
  t
```

- **Something to be careful about:** bounds on new universally-quantified polymorphism
  - *Upper bound:* Craig et al. import semantics
  - *Lower bound:* Capability-safety

E  
1



# Quantification Lifting: Type-Level Transformation

## *Benefit*

Don't need code ahead of time, only type signature

- Dynamic loading (plugins)
- Compiled code
- Third-party libraries

## *Drawback*

Over-approximation of possibly-incurred effects

# Quantification Lifting: Type-Level Transformation

*Before:*  $\tau_1 \rightarrow \tau_2$

*After:*  $\forall \varepsilon (L \subseteq \varepsilon \subseteq U) . \tau_1 \rightarrow (\tau_2)_\varepsilon$

# Related Work

## *Effect inference*

- Operates on *expressions*
- Gives exact bound on effects that can be incurred

## *Algebraic effects*

- Has a different goal
- We use the effect system to formally/statically reason about capabilities

# Observations

- **Capabilities** are good way of managing non-transitive access to system resources
- **Effect systems** can formalize capability-based reasoning, but can be verbose
- Craig et al.'s **import semantics** work great for lambda calculus
- **Quantification lifting** handles tricky interaction between effect polymorphism and mutable state

# Example Summary

```
resource type Logger
  effect log
  def append(contents : String) : {log} Unit

module def reversePlugin(name : String)
  var logger : Logger = ...
  def setLogger(newLogger : Logger) : Unit
    logger = newLogger
  def run(s : String) : String
    val t = s.reverse()
    logger.append(name + ":" + s + " ->" + t)
  t
```

```
import fileLogger, databaseLogger, reversePlugin
val logger1 = fileLogger(...)
val logger2 = databaseLogger(...)
val plugin = reversePlugin[logger1.log]("archive")
def main() : {logger1.log} Unit
  plugin.setLogger(logger1)
  // plugin.setLogger(logger2) <-- not allowed!
```

```
resource type Logger[effect E]
  def append(contents : String) : {E} Unit

module def reversePlugin[effect E](name : String)
  var logger : Logger[E] = ...
  def setLogger(newLogger : Logger[E]) : {E} Unit
    logger = newLogger
  def run(s : String) : {E} String
    val t = s.reverse()
    logger.append(name + ":" + s + " ->" + t)
  t
```

```
resource type MyPlugin
  def setLogger(newLogger : Logger') : {logger1.log} Unit
  def run(s : String) : {logger1.log} String

resource type Logger'
  effect log = {logger1.log}
  def append(contents : String) : {log} Unit
```

# Thank you for the course!



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